

## Pulsed Nuclear Magnetic Resonance

(version February 2008)

### I. INTRODUCTION

#### A. GENERAL COMMENTS

Nuclear Magnetic Resonance (NMR) spectroscopy is perhaps one of the most important scientific developments of the twentieth century. Since its discovery in the mid 1940's, NMR has found applications ranging from solid state physics and materials science to chemical analysis and biophysics. This experiment will serve as an introduction to many of the chemical and physical principles underlying such studies. While many phenomena can be explored with this apparatus, time may not allow for the completion of every exercise. In performing the lab, then, be sure to choose a wide assortment of measurements.

#### B. REFERENCES

Before proceeding, it is **essential** to become familiar with the theory and concepts governing NMR. Particular emphasis should be given to understanding Boltzmann equilibrium, the Larmor frequency, rotating reference frames, free precession, nutation by radio frequency (RF) pulses, spin echoes,  $T_1$ ,  $T_2$ , and chemical shifts. Note that without a prior comprehension of these concepts, the lab will *not* be understood at all. The material in this write-up does not substitute for reading the references.

The following publications are excellent references for this experiment:

- i. *Experimental Pulse NMR: A Nuts and Bolts Approach*, by E. Fukushima and S.B.W. Roeder. A must-read for the basics, especially pp. 1-35, 50-60, 125-139, 185-197, and 297-312.
- ii. *High Resolution Nuclear Magnetic Resonance*, by J.A. Pople, W.G. Schneider, and H.J. Bernstein. Specific attention should be given to Chapter 1 (pages 3-11), Chapter 3 (pages 22-49), and pages 50-73 and 82-86 of Chapter 4. Chapter 5 presents a fairly light introduction to the high-resolution spectra used in chemical analysis.
- iii. *Concepts in Magnetic Resonance* (John Wiley & Sons, Inc.) Vol. 12(5), 257-268 (2000). This article describes the apparatus and experiments of this laboratory exercise.
- iv. There is a good NMR text on the web by U. Hornak at <http://www.cis.rit.edu/htbooks/nmr>. Hornak has a companion text on MR

imaging at the same address (but htbooks/mri). The NMR text is available at the Physics 322 website.

## II. PULSED NMR APPARATUS: HARDWARE DESCRIPTION

The pulsed nuclear magnetic resonance apparatus used in this experiment is simple but exhibits state-of-the-art performance. Its principal components include a 14,092 gauss permanent magnet, an NMR probe, an RF receiver, an RF transmitter, and a pulse generator; data analysis and spectra acquisition is performed using a PC. For reference, a block diagram of the complete system along with circuit drawings of the probe, RF receiver, RF transmitter, pulse generator, and power supply may be found in Appendix I. The block diagram is must-reading; it is the last page of this write-up.

### A. PERMANENT MAGNET

The permanent magnet used in this experiment is manufactured by Hitachi. Having a field strength of 14,092 gauss, the magnet also obtains very high field homogeneity (i.e., field uniformity). In order to maintain field stability, the temperature of the magnet must remain at 35 degrees Celsius. An inner, proportional oven and an outer ('guard') on-off controller provide this regulation. The electronics for temperature control are at one end of the magnet. The power consumption for the magnet is well under 100 watts. The field strength determines the frequency of spin precession, which is here (for H nuclei at 14,092 Gauss) 60.00 MHz.

**Note: The Hitachi unit has no on-off switch! Leave it plugged in at all times – including the days and months of semester breaks - to keep the magnet at a stable temperature.**

To improve the field homogeneity, a set of electrical gradient coils (termed 'shims') are provided. The shim coils are attached to the NMR probe – and thus are not within viewing range. These coils do allow for gradients to be generated. A set of 9 controls on the front panel of the magnet frame permits for adjustment of field homogeneity. The most recent resonance settings have been logged in a red notebook labeled "NMR Experiment," kept with the apparatus. Fine tuning of these settings will cancel most imperfections in the permanent magnet, thereby producing an extremely homogenous field (to a few parts in  $10^8$ ).

- i. As the labeling of some of the controls suggests, each control adjusts a coefficient in a three-dimensional Taylor expansion of the field strength:

$$H_{(x,y,z)} = H_0 + a_x x + a_y y + a_z z + \dots$$

where  $a_x$  is controlled by the knob labeled x,  $a_y$  is controlled by the knob labeled y, and  $a_z$  is controlled by the knob labeled z.

- ii. In addition, there is a (very) FINE Y control, which, as the name suggests, allows for fine-tuning on Y. A FIELD SHIFT knob at the left allows the field to be changed by 0 to 0.7 gauss (approximately, a 3000 Hz range), up or down depending on the  $\pm$  switch selection.
- iii. The power supply below the shim control panel is used to power both the shims and the temperature controller board. It has 120 VAC at a few points, so keep your hands out of it.

## B. NMR PROBE

The NMR probe contains the RF coil\* that surrounds the NMR sample, used for both transmitting (i.e., flipping the spins) and receiving (i.e., detecting the precessing spins. This is accomplished by conversion of the precessing spin magnetization into a radio-frequency voltage). For greater efficiency, the coil is tuned by appropriate capacitors to 60 MHz. The impedance of the coil is transformed to be 50 ohm resistive, the industry standard value for radio-frequency equipment.

The NMR probe may be thought of as a transducer, converting between the realm of RF voltages and currents and the realm of RF magnetic fields. Loosely interpreted, then, the NMR probe may be considered as an antenna; note however that none of the energy is actually radiated.

For experiments requiring an extremely homogeneous field, the sample tube can be rapidly rotated such that each spin will more nearly feel the same time-averaged field strength. That is, each spin will spend time in regions of higher and lower field strength, so an averaging occurs. For this purpose, an air jet and air turbine wheel are used. While Hitachi originally used a small compressor to generate the air for the jet, this approach was abandoned in the Physical Measurements Lab. Rather, house air is used instead: a regulator in the Lab is permanently set to +3 psig (equivalently, 0.2 atm positive pressure). This air is connected via hoses to the barb fitting of a valve located on the front-left side of the magnet's frame. The amount of air flow into the probe may be controlled by this valve. The spinner can be temperamental; Hitachi chose their design to avoid the competitor's superior, patented design!

## C. RADIO-FREQUENCY RECEIVER

As seen in the system block diagram, the spin signal from the NMR probe is directed by the diode boxes to the Hitachi amplifier (51 dB gain,  $60 \pm 1$  MHz). The input amplifier is low-noise, as is appropriate for 10-100 microvolt signals. The signal is passed to an additional 32 dB gain amplifier through a step attenuator (0-31 dB in 1 dB step increments), which allows the overall gain to be reduced for large signals. The output of

---

\* Note that the RF coil has about a 5.5 mm diameter and is about 2mm long – a very short solenoid. This is why the field  $H_1$  is so inhomogeneous, even across small volume samples.

the 32 dB gain amplifier is at the Larmor spin frequency (the frequency at which the nuclear spins precess about their axis), or nearly 60 MHz.

The amplified signal is then frequency-shifted (heterodyned) to near zero frequency by mixing it with the 60.000 MHz crystal oscillator's output. (This oscillator is also the source of the RF transmitter.) Note that the output of the mixer (the phase-sensitive detector) has components at both the sum and difference frequencies. It is only the difference frequency that passes through the low-pass filter. Thus the NMR signal at 60 MHz  $\pm \Delta$  (where  $\Delta$  is small, since the spins are quite near 60 MHz) appears at frequency  $\Delta$ . This signal is of a much lower frequency than 60 MHz. See section III L for more on phase-sensitive detection.

In brief, the receiver amplifies the weak signals from the precessing spins and the mixer shifts their frequencies to low values. This frequency shifting makes the signal easier to see on the oscilloscope and easier to digitize for recording in the computer.

#### D. RADIO-FREQUENCY TRANSMITTER

As seen in the system block diagram, the 60.000 MHz crystal oscillator is the RF source. The oscillator's output is split, with one output going to the receiver's mixer and the other output gated by Hewlett-Packard gates. By using two gates, any leakage of RF pulses while the transmitter is in the "off" position is suppressed (if the first gate doesn't kill the leakage, the second gate will). The gating signals for these gates come from the pulse generator (as described below). To control the strength of the RF field  $H_1$  presented to the spins, the output of the gates passes through a step attenuator. The attenuator output feeds a 10 Watt (maximum) RF power amplifier; the gain control on this amplifier should remain fully clockwise.

The output of the RF power amplifier is directed to the probe through a network of diodes. These diodes collectively form the automatic Transmit-Receive (T-R) switch. Recall the V-I characteristics of ordinary silicon diodes: in the forward direction, the current  $I$  remains nearly zero until  $V$  approaches 0.5-0.7 Volts (this is termed the 'forward knee'). As a result, a pair of diodes in parallel with reverse polarity will act as a *high impedance* for *small signals* (like the 10-100 microvolts generated by the precessing spins) and as a *low impedance* for *large signals* (like the many volts from the RF power amplifier during RF pulses).

Put otherwise, for voltages greater than 0.5 to 0.7 Volts, the diode in the forward direction conducts, while for voltages more negative than -0.5 to -0.7 Volts, the reverse diode will conduct. In doing so, the diodes essentially act as shorted wires or zero impedance ('on' switch). However, if the voltage magnitude is below  $|0.5|$  Volts, neither the forward nor the reverse diode can conduct, rendering the diode assembly as 'off'. Using this model of 'on' and 'off' silicon switches, it is possible to track the signal/power flow to and from the NMR probe, in transmit and receive modes.

---

In the event that a transmitter pulse of excessive amplitude and/or duration is sent to the NMR probe, the fuse should blow before the diodes and the NMR probe are damaged (see block diagram). Because the pulse generator can put out long pulses when it is turned on or off, **the RF power amplifier should always be turned on last and turned off first**. In this way no long pulses are sent to the probe.

In summary, the RF transmitter generates RF pulses (as commanded by the pulse generator) to produce the RF magnetic field  $H_1$  in the NMR probe; it is this time-varying field that flips the spins. A network of diodes performs automatic T-R switching, allowing the same probe to be used for both transmitting and receiving.

## E. PULSE GENERATOR

The pulse generator controls both the length of the RF pulses and the spacing between them. The output of the pulse generator drives the transmitter gates and triggers the oscilloscope and/or computer used to display and/or acquire the spin signal.

This is a simple pulse generator that runs a fixed sequence. The sequence is initiated by the repetition rate generator, which sends out a triggering pulse every 0.1-100 seconds (as selected by front panel knobs). This triggers pulse 1 followed by a first delay, then pulse 2 followed by a second delay, and then pulse 3. The entire sequence repeats with the next triggering pulse as demanded by the repetition rate generator. Note that the pulse widths can be independently adjusted from 1-100  $\mu$ sec and the delays can be set independently from 0.1 msec to 10 seconds.

Each pulse (1, 2, and 3) has a separate front panel output BNC port for triggering either the counter/timer, the oscilloscope or the computer at the desired point in the pulse sequence. The output to the transmitter gates is toggle-switch selected to include pulse 1 (off-on), pulse 2 (off-on), and pulse 3 (off-on). Turning a pulse off at the toggle switch does not change the internal workings of the pulse generator; rather, the deselected pulse simply is not sent to the transmitter gates. So, for example, one could still trigger on pulse 2, even if only pulses 1 and 3 are sent to the transmitter gates.

## F. OSCILLOSCOPE

The Tektronix 2221A oscilloscope is a storage device allowing for real-time acquisition and analysis of NMR signals. To begin, select "non-storage" and use it as an ordinary scope. Start with a liquid sample, 2 ms/cm time-base, 20 mV/cm vertical base and external triggering; one trace per pulse will be generated.

For a non-blinking (stored) display, hit the "storage" button. Note that the scope has separate intensity controls for store and non-store. Throughout most of this experiment, the scope should remain in the 'stored' display. (You'll really

appreciate the storage feature - it's a lot easier to look at.) In the event the scope is not set up for storage, hit the ACQ button in the SETUP box. Hit the 4K/1K button and turn the cursor knob until "Trig Pos: 4K/1K" appears. Now hit ACQ to exit; the scope should be set to store.

Note that the Tektronix 2221A is a lot more oscilloscope than will be needed in this experiment. Once set up though, its extra capabilities do not get in the way.

## G. COUNTER

The Hewlett-Packard 5314A is a 100MHz/100ns Universal Counter. It features a seven-digit, seven-segment LED display with overflow indication, seven function performance, and full input signal conditioning. The seven functions of the counter include Frequency, Single-Shot Period, Period Average, Time Interval, Totalize, Ratio, and Self Check. These functions are accomplished by a single LSI integrated circuit. The input signal is AC coupled and can be conditioned by slope selection, trigger level, or attenuation.<sup>1</sup>

Throughout this experiment, the counter will be used to achieve enhanced accuracy in setting the pulse width and measuring pulse delays. Only the four buttons to the right of the counter should be adjusted.

In adjusting the counter settings, the objective is to trigger to start the timer on the front edge of the pulse and stop the timer on the back edge. The '+/- slope' switch controls whether the 'event' occurs when the input voltage goes up or down through the selected level. The level control is responsible for generating an event when the input signal passes the dialed-in level (DC voltage) in the direction given by the slope (+/-).

There are 2 events: one to start the counter and the other to stop. You can choose to start and stop on the same voltage source or 2 different sources (a setting marked 'SEP' for separate inputs or 'COMMON' for a single input). On 'SEP,' you could choose to measure the time interval between the + (rising) edge of a voltage input into the A BNC connector and stop on the - edge of the voltage hooked to the B BNC connector, or, conversely, you could choose to measure the interval starting on the - edge of the A input and stopping on the + edge of the B input. On 'COMMON,' you can time the interval from one edge to the other of the same voltage (input to A; no choice, it must be A).

So to measure the length of (say) pulse 1, hook the "output 1" of the pulse generator to the timer's A input. The slope settings should be + and - (left, right) and you should select COMMON.

To measure the delay between pulses 1 and 2, hook "output 1" to the timer's A input and "output 2" to B input. Select "SEP" (for separate). The delays are generally much longer

---

<sup>1</sup> As adopted from the HP 5314A Universal Counter Operating and Service Manual. For additional information, please refer to this manual, located on the table next to the magnet. The manual is also available from the 322 class web-site.

than the pulses themselves, so it matters little whether you trigger on pulse 1's rising or falling edge (same with pulse 2).

Use the N=1 setting (no averaging) and select time interval A to B (TI, A-B). The shift key (black/blue) should be on blue. The timer counts in microseconds. Leave the two level knobs pointing to the + symbol (this is in the middle of the TTL voltage range of 0 to 3 volts).

## H. COMPUTER

The computer can be used to digitize, signal average, and/or store any signal viewed by the oscilloscope. The Pentium 4 PC supports a Windows XP operating system. It has a processing speed of 1.6GHz and a memory of 128MB RAM. FIDoLite\* software, developed by Caleb Browning and Sam Gross of Mark Conradi's research group, allows one to acquire and save signal data and launch the signal analysis. FIDoLite may be accessed either from the Desktop or from the shortcut in the Start Menu.

Once the program has opened, two displays can be seen on the screen. If a sample is in the probe, hit "Acquire." The top display will output the signal seen on the oscilloscope while the bottom display will be zeroed out. This bottom graph is a remnant from the full FIDo program and is not used in this experiment. Your hardware has a single phase detector, with its output representing the spin magnetization along a particular axis in the rotating frame. The software supports two phase detectors (called in-phase and quadrature, I and Q,) along perpendicular axes in the rotating frame.

Before acquiring signal, make sure that the data directory is set to c:\FIDo\data\ . Once signal has been acquired, be sure to save the data in the 'data filename' slot. All filenames should end with the file extension '.dat'.

The *upper-limit*, *lower-limit* control adjusts the maximum and minimum voltage levels displayed on the graphs. Note that the digitizer saturates at a  $\pm 5$  Volts regardless of the value of these controls. To ensure that the signal is not clipped by exceeding the digitizer's input range, the receiver attenuation should be set such the FID fits within  $\pm 2.5$  Volts on the display.

The *trigger level* value controls the voltage required to trigger the digitizer. The trigger signal is TTL (transistor-transistor logic); thus you should use the default value of 1.6 Volts.

The *trigger slope* function determines whether the digitizer will trigger on the rising (positive) edge of the signal or the falling (negative) edge. This should remain in its default position of triggering on the negative (falling) edge.

FIDoLite also allows the user to set the dwell time (the amount of time between successive time points), the number of points (how many points will be sampled each

---

\* Note that Dr. Conradi's group plans to maintain FIDoLite for its research

acquisition), and the number of acquisitions. The phase, which determines what angle (in degrees) the incoming data will be phase-shifted, can also be adjusted. This value should remain at its default position of zero degrees.

Note that Fourier analysis is easily and quickly performed by depressing the ‘analyze’ button. Once in the analyze screen, hit ‘Fourier Transform’ to acquire the FFT spectrum. Please see section III F for more details.

For additional information regarding the FIDoLite program, a FIDoLite User’s Manual is included on the Desktop. In the event of program failure, a backup floppy disc is available. A copy of the backup disc may be obtained either from the teaching team or from Conradi’s group.

## IMPORTANT CONSIDERATIONS

### 1. Hardware Do’s and Don’ts

- i. **Always leave the Hitachi unit plugged in.**
- ii. **Do not break a sample tube in the probe. Insert and remove sample tubes with the greatest caution. If you do break one, don’t make it worse – get help.**
- iii. **Do not let foreign objects fall into the magnet’s opening. Be sure to keep the opening covered by the Plexiglas fitting at all times.**
- iv. **Besides the shim controls, do not adjust the magnet. Receive help if it doesn’t seem to be working.**
- v. **Always turn on the RF power amplifier LAST. Turn this unit off first. In fact, we recommend turning on and off only the power amplifier, oscilloscope, and counter/timer. The rest of the apparatus should remain on.**

### 2. Depth Gauges

- i. Two depth gauges are provided with the wooden sample tube holder; made of Plexiglas, these gauges allow you to insert the NMR tube and adjust the height of the air turbine wheel.
- ii. In the longer depth gauge, the distance from tube bottom to the bottom of the air turbine is 103 mm. This setting will be used in spinning the sample tubes. At this setting, the glass tube spins with its weight supported by a little Teflon disk (bearing) at the bottom of the probe. The turbine wheel stands free, so it can spin the tube.
- iii. The shorter gauge is set for 89 mm, and is used for holding the bottom of the NMR tube near the center of the RF coil. This setting is handy for putting small amounts of sample into the RF coil. Note the weight of the tube rests on the turbine, so it will not spin this way; leave the spinning-air off.

## III. PROTON NMR EXPERIMENTS



## A. SETTING UP – FINDING A FIRST NMR SIGNAL

Insert a sample of water into the probe and set the receiver attenuator to 16 dB (towards the ‘in’ direction) of attenuation and the transmitter attenuator to 13 dB. Use the 103 mm depth gauge so that this long sample extends both above and below the RF coil. The oscilloscope should be on a 5 ms/cm time-base and a 20 mV/cm vertical setting. Ensure that the vertical input of the oscilloscope is connected to the unamplified output of the low-pass filter box.

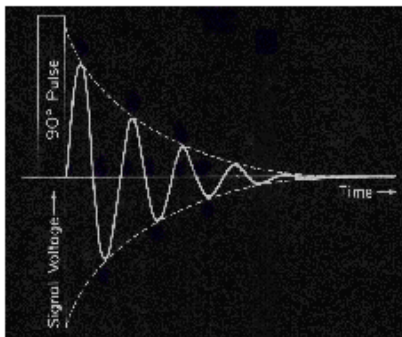
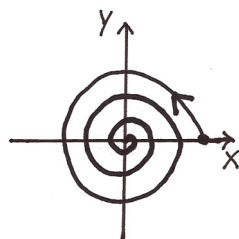
The oscilloscope should remain on 20 mV/cm. If the signal is too large or too small, change the receiver attenuator accordingly. Note, if the attenuator switch is “IN”, this means the decibels (dB) of attenuation are in the signal path (so, attenuating). If the switch is “OUT”, the attenuator is out of the path (so, no attenuation). The total attenuation in dB is the sum of all the “IN” sections. Decibels:

The number of dB =  $10 \log_{10} \left( \frac{P_{IN}}{P_{OUT}} \right)$ . So 10 dB is a power ratio of 0.1 and voltage ratio of  $1/\sqrt{10}$  (because power is proportional to voltage squared).

<u>dB</u>	<u>P-ratio</u>	<u>V-ratio</u>
0	1	1
3	2	1.414
6	4	2
10	10	3.16
20	100	10
30	1000	31.6
46	40000	200

Set the pulse generator for a repetition rate of one pulse per second; input a single pulse (make it pulse 1) of about 2  $\mu$ sec width. Note the knobs on the pulse generator have scales for approximate reading. The oscilloscope should trigger externally (external trigger source) on pulse 1.

You should see an NMR signal! To acclimate yourself with the electronics, you may want to spend some time “flying” the controls. Vary the receiver attenuation. Make the pulse width shorter and longer. Adjust the field shift control on the Hitachi shim panel; you should be able to make the displayed signal pass through zero frequency (“zero beat”). Recall the oscilloscope sees the phase detector output, which is the difference frequency between the spins and the 60.0 MHz oscillator. Try turning the shim controls to see how an inhomogeneous field leads to a more rapid decay (shorter time duration,  $T_2^*$ ) of the signal’s envelope. This free induction decay may be visualized in the following way:



*Figure 1: The FID, both as visualized in the x-y rotating frame, and as seen on the oscilloscope.*

Note that the net magnetization vector precesses around the z axis, eventually decaying to zero amplitude. It is the projection of this circular motion onto one axis that produces the decaying sinusoid.  $T_2^*$  can thus be measured by the time it takes the FID envelope to decay by  $1/e$ .

Now remove the sample from the probe for 10 seconds (a time much greater than  $T_1$ , allowing the spins to demagnetize). With  $1 \mu\text{sec}$  pulse width and a 0.4 sec repetition time, let the sample back into the probe. The signal amplitude will be observed to grow over a period of about 2 seconds, the  $T_1$  (relaxation time) of water. Note that it takes time  $T_1$  to bring the spins back into a state of equilibrium. Here you used small-angle RF pulses, so as to perturb the relaxing spin magnetization as little as possible.

Avoid overloading the receiver. Keep the output level at the unamplified output of the low-pass filter below 0.1 Volts peak-to-peak (2.5 Volts peak to peak at amplified port). Use the step attenuator to accomplish this. This limit of 0.1 Volts peak-to-peak is 5 cm peak-to-peak vertically on the scope (20 mV/cm setting).

As previously mentioned, handle the sample tubes with caution: Once the sample tubes are in the hole at the top of the probe let the tubes gently fall into place. When removing the tube, gently lift straight up.

## **B. MOTIONAL AVERAGING**

In general, the diffusive motions of the molecules in a liquid average away the dipole-dipole interactions between the spins. This averaging is absent, however, in a solid. As a result, the free induction decay (FID) has a much more rapid decay time (a smaller  $T_2^*$ ) in solids than in liquids.

The phenomenon arises because, in a solid, the presence of magnetic fields from neighboring nuclear spins causes a distribution of fields,  $\Delta H$ ; this is the dipole-dipole interaction. And, since  $\omega = \gamma H$ , this field distribution also corresponds to a frequency distribution. By the Fourier relationship (uncertainty principle)  $\Delta\omega\Delta t \approx 1$ , this range of frequencies implies a more narrow time distribution, and hence a

shorter  $T_2^*$ . Let's say it differently: assume a set of spins or oscillators with frequencies distributed over a range  $\Delta\omega$ . At  $t=0$ , they are all in-phase. It takes a time  $T_2^*$  for them to get appreciably out of phase (maybe 1 or 2 radians), with  $T_2^* = 1/\Delta\omega$ .

Use a single pulse of 2  $\mu\text{sec}$  width repeating every 2 seconds. You do not need to spin these samples. Compare the free induction decays of the following:

- i. Water
- ii. Adamantane – an organic solid where the molecules rotate freely but do not translate;  $\text{C}_{10}\text{H}_{16}$ , a tetrahedral shaped molecule.
- iii. Plexiglas – a very rigid solid with essentially no motions; polymethylmethacrylate
- iv. Rubber – which, according to NMR, seems more like a liquid than a solid
- v. Grease – also liquid-like, a swollen gel
- vi. You could also study the curing of a 2-part epoxy. Just mix the two parts together and place a small amount in the bottom of a 5mm NMR tube (make sure none gets on the outside of your tube!). Use the air turbine to hold the end of the tube near the RF coil. The 89mm depth gauge will help to achieve this end. As the epoxy cures,  $T_2^*$  should get shorter (the material becomes increasingly solid-like). Use “5-minute” epoxy and work fast so you don't waste a whole day doing this!.

In each case, it is the length of the decay ( $T_2^*$ ) in which we are interested. Note that the  $T_2^*$  of the above solids is on the order of 10-100  $\mu\text{sec}$ , while the  $T_2^*$  of water is limited by the magnet's homogeneity and is approximately 20 msec here. (This factor of 1000 is big!)

When looking at the rapidly decaying signals of solids, be sure to use a short filter time constant (1 or 2  $\mu\text{sec}$ ). To guarantee that you are seeing NMR (and not just the tuned circuit ringing of the probe), try removing the sample to see the difference. Since the Hitachi-built probe has some hydrogen-bearing solids near the coil, there is a signal with a short  $T_2^*$  even without a sample inserted, but it will be smaller than the signal of the plexiglass. You can convince yourself that you are seeing the plexiglass NMR signal by watching on the oscilloscope for the displayed signal to increase when you drop-in the plexiglass sample tube.

### C. NUTATIONS

The experimental objective in studying nutations is to examine the effect of an RF pulse upon the spins. A single pulse is applied to the sample with a repetition time much greater than  $T_1$ . In this way, the spins are allowed to return to equilibrium before another pulse of magnitude  $H_1$  is applied for a time  $t_w$  (the width of the pulse). The spins are expected to nutate (or

precess) about  $H_1$  through an angle  $\theta$  of  $\gamma H_1 t_\omega = \theta$ . Since the spin's magnetization  $M$  starts along the  $z$ -axis, the projection of  $M$  in the  $x$ - $y$  plane will be:

$$M_0 \sin \theta = M_0 \sin(\gamma H_1 t_\omega)$$

From the variation of amplitude with  $t_\omega$ , one can determine both the nutation frequency  $\gamma H_1 / 2\pi$  (where  $\gamma / 2\pi = 4.2577 \times 10^3$  Hz/gauss for protons) and the pulse widths that correspond to 90 and 180 degree pulses. You will recognize a 90 degree pulse as the pulse giving maximum FID amplitude; the 180 degree pulse produces a minimum amplitude FID following it. Note that a plot of  $M$  versus  $t_\omega$  will produce a **damped** sinusoidal oscillation. Plot this for yourself. The damping is due to the variation of  $H_1$  over the sample volume. Recall the RF coil is quite small, so its field  $H_1$  is not very uniform.

For this experiment, use the sample of glycerol (which has a very short, convenient  $T_1$  of about 0.1 sec). The amount of glycerol in the sample tube is fairly small, allowing all the spins to more nearly see the same  $H_1$ . Using the air turbine, suspend the sample tube so that the sample is close to the center of the probe's RF coil; from the bottom of the turbine to the bottom of the test tube should be 89 mm (the 89 mm depth gauge should be used to obtain this distance). Use a single pulse, repeating every 1.0 sec ( $\gg T_1$ ). Record the initial amplitude of the spin signal versus  $t_\omega$  of the pulse. Pulse width should be measured using either the oscilloscope (or a second oscilloscope) or the counter-timer. To measure the signal amplitude, be sure to get off resonance enough to provide a convenient beat note whose amplitude is easily determined. Use the field shift knob to get an FID similar to that of Figure 1.

Note that by looking at the initial phase of the signal, it is possible to distinguish between + and – amplitudes. This is easier if you are closer to resonance, since here there are fewer beats in the FID.

It is advisable to determine  $H_1$  for 3 settings of the transmitter attenuator. Keep the results handy so you can set 90° and 180° pulses for many of the later exercises.

#### D. SPIN ECHOES AND $T_2$ MEASUREMENT

Spin echoes are an interesting phenomenon, demonstrating that spectroscopic techniques can modify the system Hamiltonian. In the spin echo, the 180 degree pulse positions the spins as though they ran backwards between the two pulses.

A spin echo is formed using a two pulse sequence, consisting of a 90° pulse followed by a delay  $\tau$  and then a 180° pulse. If the net magnetization vector is assumed to be initially oriented along the  $z$ -axis, the  $\pi/2$  pulse (along  $x$ ) will rotate the magnetization by 90 degrees to the  $-y$ -axis. During time  $\tau$  between the first and second pulse, the different spin packets will freely evolve (or dephase) in the  $x$ - $y$  plane because they see slightly different static fields  $H$  and precess at slightly different frequencies  $\omega = \gamma H$ . The  $\pi$  pulse then rotates each magnetization vector

180° about the x-axis of the rotating frame, leaving the vectors again in the x-y plane. After a further time  $\tau$ , the magnetization vectors are back in phase along the y-axis and an echo is observed (see *Experimental Pulse NMR: A Nuts and Bolts Approach* for a good discussion complete with figures).

In this exercise, the behavior of the spin echo will be used to determine  $T_2$  of glycerol. Use the depth gauge and put the short sample of glycerol in the probe at the correct height (89 mm). Select two pulses set to 90° (pulse 1) and 180° (pulse 2). Space the pulses by  $\tau = 5$  msec, say, to start. Un-adjust the shim controls to make a rapid decay (short  $T_2^*$ ), easily achieved by mis-adjusting the z-shim by a couple of turns on the knob. Don't forget to record the "correct" setting so you can return to it. Tune onto resonance (use field shift knob) so a rapidly decaying FID is seen after pulse 1 and you will see a similar but inverted spin echo at time  $\tau$  after the second pulse. Use 1.0 sec repetition time and trigger on the first pulse.

You should see an FID after pulse 1, possibly a weak FID after pulse 2, and a spin echo at  $2\tau$  after the first pulse. Try varying the spacing  $\tau$  to see that the echo really does occur at time  $2\tau$  (measuring from the first pulse). For fixed  $\tau$  vary the first and second pulse widths to obtain maximum echo amplitudes. These pulse widths should correspond to 90° and 180° nutations, as found in part C. Plot the echo amplitude  $M$  on a log scale as a function of  $2\tau$ . A nearly exponential decay obeying  $Ae^{-2\tau/T_2}$  will be observed. Determine  $T_2$  of glycerol.

You can use linear graph paper to plot  $\log M$  as a function of  $2\tau$ . If  $M$  is the echo amplitude and

$$M = A \exp(-2\tau/T_2), \text{ then}$$

$$\ln M = \ln A - (2\tau)(\frac{1}{T_2}). \text{ This is of slope -intercept form, } y = b + mx,$$

where  $y = \ln M$ ,  $x = 2\tau$  and the slope  $m = -1/T_2$ .

Likewise, the three-pulse sequence  $\pi/2 - \tau - \pi/2 - T - \pi/2 - \tau - \text{echo}$  (with  $T > \tau$ ) creates a stimulated echo at time  $\tau$  after the third  $\pi/2$  pulse. Again it is assumed that the net magnetization vector is initially oriented along the z-axis. This equilibrium z-magnetization is transferred to transverse magnetization by the first  $\pi/2$  pulse. During free evolution of length  $\tau$ , the magnetization dephases. The second  $\pi/2$  pulse rotates the magnetization vectors into the xz plane. During time  $T$ , the transverse magnetization decays, while  $M_z$  stays constant (no precession since it is parallel to the field). At time  $t = T + \tau$ , the third  $\pi/2$  pulse transfers the z-magnetization pattern again to transverse magnetization which forms an echo at time  $t = T + 2\tau$  along the +y-axis.

Roughly speaking, the  $\pi/2 - \tau - \pi/2 - T - \pi/2 - \tau - \text{echo}$  sequence is a 90-  $\tau$ -180-  $\tau$ -echo where the 180 is broken into two 90° pieces spaced by  $T$ . During this "time-out," the spin magnetization component parallel to  $z$  does not precess, so that the interval  $T$  does not affect the echo formation: Try varying the delay intervals and see if you

can identify all the FIDs and echoes you see. We recommend the three pulses be 45, 45, and 90 degrees, to best see all the echoes. Try turning off one or more of the RF pulses (toggle switches on the pulse generator) to check yourself-the 1-3 echo (FID following pulse 1 refocused by pulse 3) will not disappear when pulse 2 is switched off, though the 1-3 echo may change amplitude. When pulse 1 is off, you will see an echo of the FID following pulse 2, refocused by pulse 3. It may help to keep these echoes apart from each other in time. We recommend using a first delay of 5 ms and a second delay of 15 ms. You may need to reduce the field uniformity (z shim knob) so the FIDs and echoes are short and do not run into each other.

## E. MEASURE RELAXATION TIME $T_1$

This exercise will allow you to measure the spin relaxation time  $T_1$  - i.e., the time it takes the system to return to equilibrium – using two distinct methods: Saturation-Recovery and Inversion-Recovery. Measure  $T_1$  for any of the following samples:

- i. Glycerol
- ii. Rubber
- iii. Grease
- iv. Solid Adamantane
- v. A solution of water with dilute cupric ion (paramagnetic). Note that the  $T_1$  of any substance is shortened by the large magnetic moment of paramagnetic ions. Paramagnetic here means that the ion has a net unpaired electron spin. In most substances, all the electron spins are paired anti-parallel, leading to cancellation.

Saturation uses a two-pulse sequence consisting of a  $90^\circ$  pulse followed by a delay  $t$  and then another  $90^\circ$  pulse ( $90^\circ$ - $t$ - $90^\circ$ ). The FID following the second “inspection” pulse is proportional to the z-magnetization ( $M_z$ ) just before the pulse. Thus by measuring the amplitude of the FID following this pulse, we inspect the Z-magnetization just prior to the pulse. In order for the FID to decay rapidly (to prevent one FID from running into the next), the z-shim may be un-adjusted. Trigger the scope on the second  $90^\circ$  pulse so that the FID from pulse 2 is observed. Both pulse 1 and pulse 2 should be switched on at the pulse generator.

Vary the time  $t$  using the first delay’s knobs; watch the FID amplitude change as you do. The FID signal amplitude  $M$  will vary as

$$M_{(t)} = A (1 - B \exp(-t/T_1)).$$

For a perfect first  $90^\circ$  pulse,  $B=1$ .

If  $t \gg T_1$  (this  $t$  can be regarded as infinite),  $M=A$  so

$$M \infty - M_{(t)} = AB \exp(-t/T_1). \text{ Taking the natural log of both sides,}$$

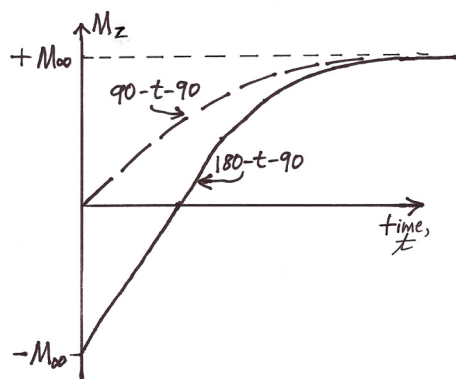
$$\text{Ln } [M \infty - M_{(t)}] = \text{ln } (AB) + (-1/T_1) t.$$

We recognize this as slope –intercept form,  $y = b+mx$ , where  $y = \ln [M_{\infty} - M(t)]$  and  $x=t$  and slope  $m=(-1/T_1)$ .

Notice that it is important to measure  $M$  for a long delay time to get “ $M_{\infty}$ ”. You may recall that for  $t > 5T_1$ ,  $\exp(-t/T_1)$  is less than 1%. You might also be impressed that our analysis in terms of the slope makes the value of  $B$  unimportant. That is, the first pulse need not be exactly  $90^\circ$ .

Inversion recovery uses a  $180^\circ$ -  $t$  - $90^\circ$  (inspect) sequence to determine relaxation time. The first pulse inverts  $M_z$ ;  $M_z$  then recovers towards equilibrium during the interval  $t$ . The second  $90^\circ$  pulse tips whatever magnetization is along the  $z$ -axis into the  $x$ - $y$  plane. The resulting signal just after the  $90^\circ$  pulse is proportional to the  $z$ -magnetization just prior to the pulse.

Therefore, the signal amplitude will vary again as  $A(1-Be^{-t/T_1})$ , with  $B=2$  for ideal  $180^\circ$  pulse. See Figure 2. By plotting  $M_{\infty}-M(t)$  on a log scale, one again obtains a straight line with slope  $-1/T_1$ . When using the  $180^\circ$ -  $t$  - $90^\circ$  sequence, be sure to wait at least  $5T_1$  between repetitions of the experiment. Otherwise, the magnetization coming into the sequence will be less than the equilibrium value  $M_{\infty}$ . That is, you want your  $180^\circ$  pulse to work on the full, 100% recovered magnetization. So you let the spins recover (at least 5 times  $T_1$ ) before doing the next  $180^\circ$  and  $90^\circ$  pulses. By the way, this tedious waiting is not required for  $T_1$  measurement by  $90^\circ$ - $t$ - $90^\circ$ . After all, any magnetization that recovers between the one  $90^\circ$ - $t$ - $90^\circ$  and the next is just slated for death ( $M_z=0$ ) by the next  $90^\circ$  pulse.



*Figure 2: How the magnetization  $M_z$  varies just after the  $90^\circ$  pulse in the  $180^\circ$ -  $t$  - $90^\circ$  (inspect) sequence (solid curve) and  $90^\circ$ - $t$ - $90^\circ$  (dashed curve). The plot also gives the amplitude of the FID following the second pulse. The role of the second pulse is to convert  $M_z$  into observable NMR signal.*

## F. CHEMICAL USES OF NUCLEAR MAGNETIC RESONANCE

In recent years, Nuclear Magnetic Resonance has become an indispensable analytical tool in chemistry. The chemical applications of NMR range from analyzing the content and purity of a sample to determining its molecular structure. NMR can quantitatively analyze mixtures containing known compounds. For unknown compounds, NMR can

either be used to match against known spectral collections (tabulated in books or on-line) or to infer the molecular structure directly. Once the basic structure is known, NMR can be used to determine molecular conformation in solution; it can also be used to study physical properties at the molecular level, including conformational exchange, phase changes, solubility, and diffusion.

We note, for example, that the Washington University Chemistry Department has approximately 4 NMR machines for analysis of reaction products. This translates into a 2 million dollar investment. Nationwide, the monetary total of all NMR instruments is perhaps 1 billion dollars (!).

This exercise will lead you through the basics of chemical NMR spectroscopy.

So how does chemical NMR spectroscopy work? Consider for example a simple (and perhaps all-too-familiar) molecule:  $\text{CH}_3\text{CH}_2\text{OH}$ , ethanol. This compound has three types of hydrogen nuclei including  $\text{CH}_3$  (methyl),  $\text{CH}_2$  (methylene), and  $\text{OH}$  (hydroxyl). For each of these, the resonance frequency is proportional to the field  $H_n$  at the nucleus:

$$f = (\gamma/2\pi)H_n$$

And the field at the nucleus  $H_n$  is made up of the external field  $H_o$  from the magnet and a weak field from the nearby electrons:

$$f = (\gamma/2\pi) (H_o + \Delta H)$$

Now  $\Delta H$  is due to weak currents in the electronic cloud induced by the external field (similar to eddy currents). So,  $\Delta H$  is proportional to  $H_o$ :

$$\Delta H = -\sigma H_o$$

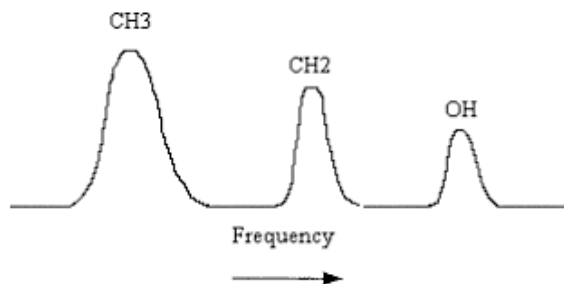
Note that the negative sign is incorporated into the definition by convention. Thus,

$$f = \gamma H_o(1 - \sigma) / 2\pi$$

Here,  $\sigma$  is called the chemical shift; for protons, the range of chemical shifts is about 0-10 parts per million. These shifts are *small*!!!! NMR was around for a few years before the shifts were observed. Basically, the early magnets were not uniform in field, so the NMR lines were too broad.

However – and here's the good part – even though  $\sigma$  is small,  $\sigma$  is different for each type of hydrogen nuclei. Thus, in the same external field  $H_o$ , the  $\text{CH}_3$ ,  $\text{CH}_2$ , and  $\text{OH}$  protons (hydrogen nuclei) have three slightly different frequencies. The Fourier spectrum should look like:





*Figure 3: From left to right the peaks with increasing frequency are CH<sub>3</sub>, CH<sub>2</sub>, and OH, with the intensity ratio 3:2:1 (ratio of areas in the spectrum) arising from the relative numbers of each kind of proton.*

Note that for ethanol, the overall width of the spectrum is about 4 parts per million. At a 60 MHz frequency, this implies that the spectrum is only approximately 240 Hz wide. If the field  $H_0$  is not extremely homogeneous (ppm or better), then each line will be so broad that it merges with the next. This is why it is of utmost importance to have a uniform field.

Let's get started. To shim (i.e., improve the homogeneity of) the magnet, use a single pulse of about 1  $\mu$ sec every 0.5 seconds. Use a transmitter attenuation of 13dB. Such settings correspond to a small tip angle so that the experiment can be repeated faster than once per  $T_1$ . More formally, the small pulse barely perturbs the magnetization because the cosine of a small angle is nearly 1. Use the water sample, suspended in the probe a distance of 103 mm (use the depth gauge). As will be seen, the water sample has only a single resonance line; all the H nuclei are equivalent.

## G. SHIMMING

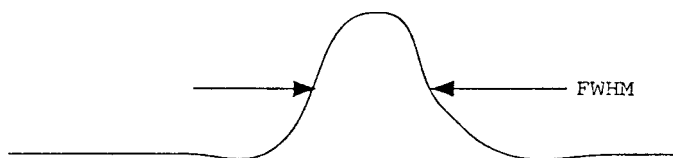
By adjusting the shim controls, you can make the water FID extend further across the oscilloscope screen to the right (longer  $T_2^*$  means better field uniformity as it takes longer to de-phase when the spins all run at more nearly the same frequency). Start with the settings in the logbook, or the settings from the last group of students (assuming they were successful).

Initial adjustment is done on  $x$ ,  $y$ , and  $z$  with the sample tube not spinning. Go over these in a loop 3 times. Now turn on the spinner-drive air and make sure the sample is indeed spinning. With the sample of water spinning smoothly (in truth, the spinner turbine and bearing are the least robust parts of the apparatus; be forgiving), and having already set  $x$ ,  $y$ , and  $z$  on the non-spinning sample, the important controls are  $y$  (or fine  $y$ ) and curvature (with the uninformative label "B"). Maximize the duration of the FID using fine  $y$ ; then try a new setting of B by 10 or 20 points (i.e., 0.1 or 0.2 turns on the knob), again optimizing fine  $y$ .

With  $y$  (or fine  $y$ ) and B adjustments, you should be able to make the water FID last 0.5 seconds or so, with a  $1/e$  decay time of perhaps 0.2 seconds, corresponding to a frequency width (see below) of about 2 Hz. 2 Hz out of 60 MHz means the field is uniform to about 3 parts in  $10^8$ , which is remarkable.

Note: as you make the field more uniform and the FID grows longer in duration, you will want to increase the repetition time, so that one FID is fully decayed before you hit the next rf pulse. This might mean 1 pulse every 3 seconds. Patience is suggested.

Make sure to record your settings in the log book, to help keep track of changes (it helps the next group of students). And if you turn the wrong knob, you'll be glad to have recorded the optimum settings, so your error is easily corrected.



*Figure 4: This figure depicts the full width at half maximum (FWHM) of a resonance line.*

You can now use the FIDoLite software to capture the FID and perform a FFT on the FID, outputting the Real and Imaginary parts each as a function of frequency. Be sure to save the FID and the final Real and Imaginary FFT files with the extension '.dat.' To view and print the files, you can access the data arrays from EXCEL. First, from EXCEL, open the directory the data is saved in (should be c:\FIDo\data\). Then choose file type as delimited, hit 'next', and set delimiters as tab. The worksheet will display all numerical values associated with the signal and spectrum. To graph the data, simply create a new chart in the EXCEL worksheet.

Acquire one FID (no averaging needed-these are big signals) and Fourier transform (FT) it - you'll see a single line because  $\text{H}_2\text{O}$  has all equivalent hydrogens. (Your FT software package cannot distinguish + and - frequencies, so the spectrum will have mirror symmetry about the origin). And there may be an even bigger line at zero frequency if you did not correct the baseline of the data.

How to FT: Now is a good time to teach you how to FT properly. First, choose a dwell time (DW, time per point) which is short enough that you properly sample the highest frequency component of the signal (look at FID on scope). The Nyquist criterion is that the highest frequency sine (or cosine) needs at least 2 samples in each cycle. Typically, the dwell might be 100  $\mu\text{s}$  to 1 ms.

Next choose the number of acquired points N so that the total time duration T of the acquired data set is long enough to fully capture the signal; the signal should decay fully in the first ~30% of the time. T determines the "digital frequency resolution", with the frequency-domain points (i.e., after Fourier transformation) spaced by  $1/T$ . Let's say you want 0.25 Hz spacing in frequency, so your time-domain data set must be  $T \sim 4$  seconds long. At a dwell  $\text{DW} = 1$  ms, this is  $N=4000$  points (FIDo knows  $2^n$ , so it will make this  $N=4096$ ), a manageable data set. But if you chose  $\text{DW}=10$

$\mu$ s, you'd need 100 times as many points and you'd quickly run out of disk space. As a guide, you will never need N to be greater than  $16K = 16,384$ .

After acquiring the data (usually the signal-to-noise is great, so one acquisition or average is plenty), go to the ANALYZE feature of FIDo. Under TRANSLATION CONTROLS, put-in the baseline window (for removing any dc additive offset from the data). Use the last 25% of the data points (so for  $N=4096$ , go from 3000 to 4000). Hit the button "Baseline" to do it; here "Baseline" is an imperative verb.

Get out of this screen (use the OK button at the bottom) and hit the Fourier Transform button. The spectrum will show lines mirrored about zero frequency; just pay attention to the positive frequency side. If you have baselined correctly, there should not be a spike at zero frequency. For water, there should be just one resonance line (except for the mirror image).

Phasing: Go to Phase Adjust and adjust the "constant phase" correction, leaving the "linear" correction at zero. Adjust until the upper display looks like in Figure 4.1.

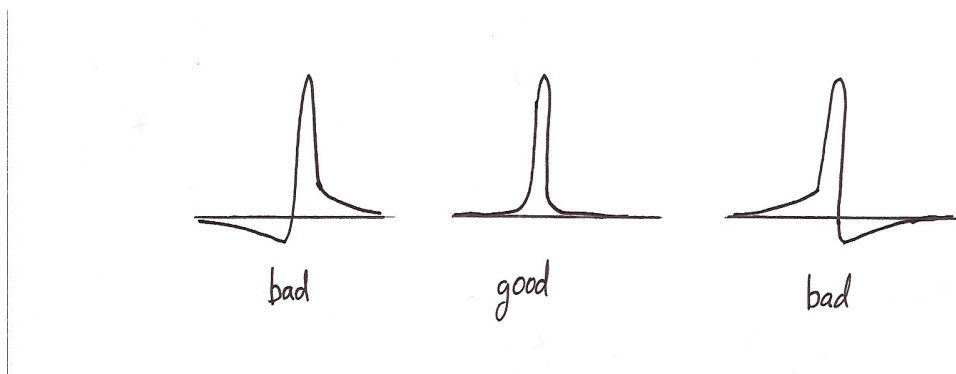


Figure 4.1 Phasing of lineshape.

The idea is that the curve should not have negative regions.

Now put in ethyl alcohol. The FID is much more complicated because there are 3 lines (more than 3, if one considers the J-couplings). Capture the FID in the computer, FT the signal, and display. You'll see 3 lines (or 3 groups of lines), like Figure 3. Because of the  $\pm$  frequency ambiguity, you'll want to use the FIELD SHIFT knob (Hitachi shim panel) so that all 3 lines are either all above or all below 0 (this means the 3 sets of spins are above or below the 60.000 MHz source that drives the receiver's mixer). Once all 3 lines are on the same side of 60.000 MHz, the spacing between them will be independent of the field shift.

But there's more to be seen! If you have not already shimmed on spinning water, do it now. Put the  $H_2O$  back in and turn on the spinning air. It's desirable to have the tube spin at a rate of about 30Hz, which is faster than the human eye can follow. On this valve, about 1/4 turn will be fully open and will provide fast spinning. The  $H_2O$  FID will be much longer, so you'll need to go to a longer oscilloscope time base. Touch up the Y control (or FINE Y) to improve things a bit more. You should

be able to make a  $T_2^*$  of order 0.2 sec, corresponding to a 2 Hz line width (1/30 ppm).

Put the ethyl alcohol back in and get it to spin. Use the computer to take the spectrum. You'll see each of the lines is split by spin-spin, or J, couplings, as in Figure 4.2.

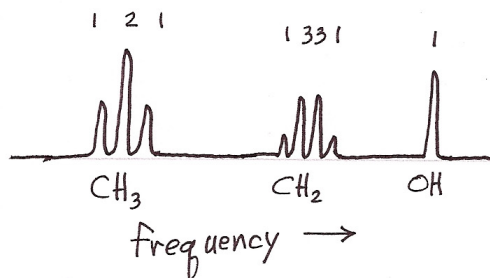


Figure 4.2 Ethanol, with added acid.

The frequency of the CH<sub>3</sub> protons depends slightly on whether the CH<sub>2</sub> protons are both up, one up and one down (twice as likely), or both down. Hence the CH<sub>3</sub> resonance is split into a 1-2-1 pattern, with a J splitting of about 5 Hz. Likewise the CH<sub>2</sub> protons have a frequency which depends on the states of the CH<sub>3</sub> protons. Thus the CH<sub>2</sub> protons show they are interacting with 3 protons by the 1-3-3-1 pattern. In other words, the 3 H's can be all up, two up and one down (3 ways), two down and one up (3 ways), or all down. Under many conditions, the OH protons exchange rapidly between different alcohol molecules. Thus the OH proton shows neither J couplings nor gives rise to J-couplings of the other protons. This is another kind of motion averaging. The ethanol sample with a bit of added acid has rapid exchange of OH hydrogens on the molecules. This is the simplest case. The sample of dry alcohol (no water nor acid to catalyze hydroxyl exchange) shows J-couplings by the OH (of the CH<sub>2</sub> signal) and J-coupling of the OH signal by the CH<sub>2</sub> hydrogens.

Another simple spectrum is ethylbenzene, H<sub>3</sub>C-CH<sub>2</sub>-C<sub>6</sub>H<sub>5</sub>. The C<sub>6</sub>H<sub>5</sub> has the benzene-ring structure. The resonance spectrum shows J-couplings between the CH<sub>2</sub> and CH<sub>3</sub> protons. The ring protons are shifted up-frequency because of currents induced in the ring. The ring protons (there are 5) do not show J-couplings to the CH<sub>2</sub> or CH<sub>3</sub> - they are too many bonds away.

Take a look at another sample-tetramethylsilane (TMS, (CH<sub>3</sub>)<sub>4</sub>Si). This compound shows a single line. There are J-couplings between the protons, but a famous theorem states that J-couplings cannot be observed between equivalent nuclei. This theorem also explains the absence of J-couplings in the spectrum of H<sub>2</sub>O.

Another sample is 2,2,2-trifluoroethanol ( $\text{F}_3\text{CCH}_2\text{OH}$ ). Here there are separate lines for the  $\text{CH}_2$  and OH resonances. The  $\text{CH}_2$  resonance will be split by the three  $^{19}\text{F}$  spins ( $S=1/2$ ). Thus, one expects a 1-3-3-1 pattern for the  $\text{CH}_2$  protons. It is a simple proof that the  $^{19}\text{F}$  nucleus has spin one half. If  $^{19}\text{F}$  were spin-zero, there would be no splitting of the  $\text{CH}_2$  resonance. Work out the patterns if  $^{19}\text{F}$  were spin-1 or spin-3/2.

A related sample is 2-iodo-1,1,1-trifluoroethane ( $\text{IH}_2\text{CCF}_3$ ). Here the  $\text{CH}_2$  protons are the only protons on the molecule. You'll see a 1-3-3-1 pattern from J-coupling between the  $\text{CH}_2$  protons and the three  $^{19}\text{F}$  spins. There is, however, no J-coupling between the  $\text{CH}_2$  protons and the iodine ( $^{127}\text{I}$ ,  $s=5/2$ ), even though they are only two bonds separated (I-C-H). The reason is the  $^{127}\text{I}$  has a large electric quadrupole moment, resulting in a very fast  $^{127}\text{I}$   $T_1$ . Thus the  $^{127}\text{I}$  are rapidly jumping between the levels  $m=-5/2, -3/2, -1/2, 1/2, 3/2, 5/2$ . This averages the J-splittings to zero, yet another example of motional narrowing. But here it is the **spin** coordinate which is moving, not a spatial coordinate.

Reviewing, we have seen motional averaging to reduce the line width in liquids (less than 1 Hz) from the huge width (40 KHz) in the solid-state, averaging of J-couplings by OH groups hopping from one ethanol molecule to the next, averaging of J-couplings to  $^{127}\text{I}$  nuclei (by the fast  $T_1$  of this spin), and averaging of an inhomogeneous (non-uniform) magnetic field by spinning of the sample.

## H. SPINNING SIDEBANDS

Put the  $\text{H}_2\text{O}$  sample in the probe and shim the magnet for longest  $T_2^*$  (non-spinning). Use 1 short pulse (1  $\mu\text{sec}$ ) every 1.0 seconds. Keep the signal below 100 mV peak to peak (unamplified port of low-pass filter). Now turn on the spinning air and  $T_2$  will get much longer. Adjust Y or FINE Y to optimize. You will want to slow the repetitions to one every 5 seconds. Now use the computer to take the freq spectrum (i.e., acquire the FID with the computer, FT it, and display the spectrum). You'll see a single, sharp resonance.

You may notice small periodic modulation in the FID envelope (adjust the FIELD SHIFT away from zero beat so the envelope is easily seen). This modulation is from the spinning. Record the optimum setting of the Z-shim. Now change Z to make the modulation more evident. Notice that the modulation is small for the correct Z setting and the modulation grows deeper (the envelope decays closer to zero) as Z is changed away from the optimum setting.

Here's the physics: in a Z-gradient, the spins will de-phase more rapidly. But when you rotate the sample about the y-axis, any spin sees exactly zero time average field (from the Z-gradient) after an integer number of revolutions. That is, a spin may be in a region of extra large H field for a while, and later an extra small H field. After  $360^\circ$  of revolution, all the field from the Z-gradient averages to zero. So the spins are all back in phase after 1, 2, 3,...n revolutions of the sample tube.

The math: for a z-gradient, of strength G gauss per cm,  $H = Gz$ . Here we omit the constant magnetic field (we are doing this in the appropriate rotating frame). For a spin at radius r from the center-line and initially at angle  $\Theta$  about the axis,  $z = r \cos(\omega t + \Theta)$ . Here  $\omega$  is the angular frequency of the tube rotation. Thus the spin sees  $H(t) = rG \cos(\omega t + \Theta)$ . The spin's precessional phase  $\Phi$  obeys  $\gamma H = d\Phi/dt$ . Thus

$$\Phi = \int_0^t \gamma H(t') dt'$$

So we have:

$$\Phi = \gamma r G \int_0^t \cos(\omega t' + \Theta) dt' = \frac{\gamma r G}{\omega} \sin(\omega t' + \Theta) = \frac{\gamma r G}{\omega} [\sin(\omega t + \Theta) - \sin \Theta].$$

Clearly, if t corresponds to an integer number of revolutions, the periodic nature of the sine function will cause  $\Phi = 0$ . The spins get back in phase every integer number of revolutions. These re-phrasings have been termed ‘spun-echoes.’ Get it?

For really large z-gradients, the spins will quickly de-phase after each ‘spun echo’. The FID will appear as a series of narrow pulses across the screen.

Send the FID to the computer and examine the FT. For small modulation, you'll see the original resonance (“center-band”) flanked by two spinning sidebands. The sidebands are separated by the sample tube’s rotation frequency (typically 30 Hz).<sup>\*</sup> These sidebands are just like those of AM radio. For the case of a large z-gradient producing sharp, well-separated echoes, there are several sidebands on each side. They are also each separated by the spinning frequency.

## I. THE MATHEMATICS OF SIDEBANDS

To understand sidebands, it is useful to understand the math relevant to AM radio. Consider a signal

$$f(t) = \cos \omega_o t (1 + a \cos \omega_m t)$$

Here  $\omega_o$  is the carrier frequency and  $\omega_m$  is the much smaller modulation frequency. The term in parentheses is “the modulation”. Expanding,

$$f(t) = \cos \omega_o t + a \cos \omega_o t \cos \omega_m t$$

Recall that

---

<sup>\*</sup> If you want, you could put a black dot or stripe on the turbine wheel and measure its frequency with a strobe light. The Physics 117-118 technical assistant has a strobe.

$$\cos(x)\cos(y) = (1/2)\cos(x+y) + (1/2)\cos(x-y)$$

So the expression for  $f(t)$  becomes

$$f(t) = \cos\omega_0 t + (a/2) \cos(\omega_0 + \omega_m)t + (a/2)\cos(\omega_0 - \omega_m)t$$

Hence the signal  $f$  is composed of 3 pieces: the carrier at frequency  $\omega_0$ , the lower sideband at  $\omega_0 - \omega_m$  and the upper sideband at  $\omega_0 + \omega_m$ . The amplitude of the sidebands is proportional to the depth of modulation  $a$ . In AM broadcast radio, the maximum allowed modulation frequency is 5 KHz, leading to a 10 KHz bandwidth. The channels are thus separated by 10 KHz.

FM sidebands are almost as easy. A typical FM signal is  $f(t) = \cos(\omega_0 t + a \cos\omega_m t)$ . The  $a \cos\omega_m t$  is a phase shift of the carrier. The phase of the oscillating signal is varied; a time change of phase is a frequency shift. Complex notation makes the math easier. So we look at  $g(t) = e^{i(\omega_0 t + a \cos\omega_m t)}$ . Looking at the last term, the argument  $a \cos\omega_m t$  is bounded by  $\pm a$ . So if  $a$  is small, we can Taylor expand

$$e^{ix} = 1 + ix + (-x^2/2) - \dots$$

which makes  $g(t)$

$$g(t) = e^{i\omega_0 t} (1 + i a \cos\omega_m t - (a^2/2) \cos^2 \omega_m t + \dots)$$

Using the definition  $\cos\omega t = \frac{1}{2}(e^{i\omega t} + e^{-i\omega t})$  and recalling that

$$\cos^2 \omega_m t = (1/2) (1 + \cos 2\omega_m t) = 1/2 + (1/4)(e^{i2\omega_m t} + e^{-i2\omega_m t})$$

we find:

$$g(t) = \left( \frac{4 - a^2}{4} \right) e^{i\omega_0 t} + \left( \frac{ia}{2} \right) \left[ e^{i(\omega_0 + \omega_m)t} + e^{i(\omega_0 - \omega_m)t} \right] - \left( \frac{a^2}{8} \right) \left[ e^{i(\omega_0 + 2\omega_m)t} + e^{i(\omega_0 - 2\omega_m)t} \right]$$

These terms are the carrier, the first sidebands ( $n=\pm 1$ ) and the second sidebands ( $n=\pm 2$ ). Note that for a small 'a,'  $a^2$  is negligible so the signal is essentially just the carrier and first sidebands. When  $a$  is big, you need to keep all the terms in the expansion, so there are 3<sup>rd</sup>, 4<sup>th</sup>, ... sidebands. The correct math for this is the Bessel functions.

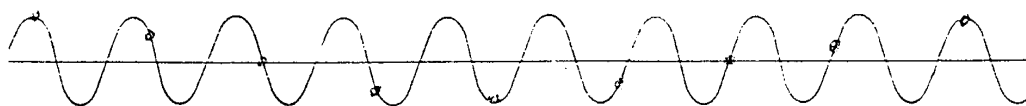
## J. A NOTE ON FOURIER TRANSFORMATIONS

The receiver provided here has a single phase-sensitive detector (mixer). Its output signal is, essentially, proportional to a component (x or y or in-between) of the precessing magnetization in the x-y plane. Because the mixer reports the difference

frequency (between the spins and the 60.000 MHz reference), the voltage gives the magnetization component in the rotating frame.

Consider a vector rotating in the x-y plane. Any one component, (x, y, or other) simply oscillates. With only one component, one cannot tell which sense of rotation (clockwise or counter clockwise) the vector has. In terms of NMR, one cannot tell whether one is above or below the 60 MHz reference. Thus, one wants to adjust the field shift so that all the NMR lines are on the same side of 60 MHz, removing the ambiguity.

But if you shift the field too far, you are asking the computer to digitize a high frequency signal. Please be aware that the computer (and all digital storage oscilloscopes) digitize the signal at evenly spaced times. Thus, if the input signal exceeds the sampling rate the situation below can occur:



*Figure 5: Sine wave input to the digitizer where the input frequency is greater than the sampling rate. The dots represent sampling instants. Even though a high frequency signal is involved, the digital oscilloscope will show a low frequency (the difference between the signal and sampling frequencies). This is called aliasing.*

Thus, it is imperative that the Nyquist criterion not be exceeded when sampling. The Nyquist criterion dictates that the signal frequency cannot exceed half the sampling rate. If the field is shifted too far, signals will appear at alias frequencies. One way to avoid aliasing, then, is to keep the NMR frequencies close to the 60.0 MHz reference frequency. But then you risk not knowing which side (above or below) the spin frequencies are. A second way is brute force, using a very high sampling rate (1 sample every 5  $\mu$ s, say, so the dwell time DW is 5  $\mu$ s). But then you will have a huge data set and you'll eat up the computer's disk space. For example, to record with 4 second acquisition duration (0.25 Hz per point after Fourier transforming) would require  $8 \times 10^5$  data points!

## K. NMR IMAGING, MRI

Perhaps one of the most influential applications of Nuclear Magnetic Resonance is MR-imaging, which relies upon the large water content of the body. The concept is simple. Since human constitution is nearly 70 percent water, in a uniform field the body will show a single resonance line. Note that the more interesting organic/biological compounds in our system do have non-trivial spectra, but their concentrations are much lower than that of water.



If a gradient field is applied from head to toes (the y direction), each horizontal plane in the body will have a different resonance frequency. Thus, spins' y-coordinates have been labeled by their NMR frequencies. If our physiology were one-dimensional, NMR imaging would be no more complex than acquiring the spectrum in the presence of the gradient and converting the NMR frequency back to the y-coordinate using

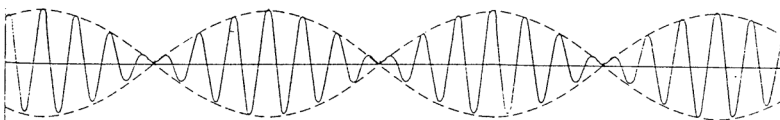
$$f = (\gamma/2\pi)H = (\gamma/2\pi)(H_0 + Gy)$$

However, since we are 3 dimensional, real imagers use gradients along X, Y, and Z, all three, switching them on and off within each pulse sequence. The method employed is called 'spin-warp' imaging, and was involved in R.R. Ernst's Nobel Prize in chemistry in 1992.

It is interesting to note that an ordinary x-ray is a projection of a 3-dimensional body into two dimensions: there is thus no way to distinguish objects in front of or behind each other. This is true of any shadowgram. And yet, these simple pictures are of considerable diagnostic value. Since static magnetic fields and RF pulses have been found not to injure living organisms, MR-imaging is competing with x-ray tomography as a main diagnostic tool in medicine.

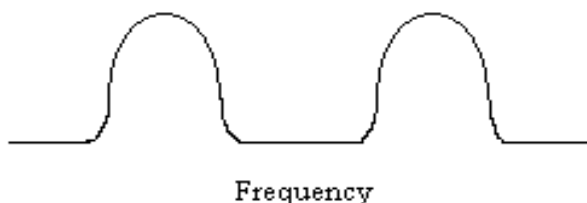
To illustrate the fundamentals of MR-imaging, we'll content ourselves with 1-D images of some simple 'phantoms' (test samples). The wood sample tube holder should contain two NMR tubes that have (glued inside) two small water capillary tubes. Use the one with the wooden dowel inside. Put it in the NMR probe with the tubes spaced along z (from pole face to pole face, or along the longest direction of the magnet assembly).

Use a single 90-degree pulse every 6 seconds. To produce a large gradient, turn the z control to one extreme or another (i.e., if it's normal setting is 865, turn it to 000; if normally below 500, turn it to 999). Use a FIELD SHIFT of about 700 or 800 (7 or 8 turns from 'zero-beat'). As seen in figure 6, a signal reminiscent of Young's double slit should be observed. (Indeed, there is a physical and mathematical connection between imaging and diffraction!) The FID envelope shows a beating or interference of the signals at the two frequencies.



*Figure 6: Beat pattern expected from the two NMR tubes in slightly different magnetic fields caused by the field gradient.*

Send this signal to the computer and perform a Fourier analysis. As depicted



*Figure 7: Frequency spectrum of the sample of two capillaries in a z-gradient*

in figure 7, the projection of the phantom onto the z-axis will be observed.

Now turn the phantom  $90^\circ$  so that the two capillaries have the same z coordinate. The two peaks will merge. Compare the image of the two capillaries with the image of the 5mm outer-diameter tube of water (about 4.2 mm inner diameter). Do the dimensions make sense compared with the NMR images?

Note that the glass tubes and the water have small but non-negligible magnetic susceptibilities. Thus, each tube provides a gradient across the other tube. To minimize this, we are using the largest possible external gradient that the magnet can provide. Nevertheless, you will still notice that one peak is less tall and broader than the other.

Now let's consider NMR imaging: if one images humans in terms of number of protons per cubic millimeter, there is not much contrast. Most body tissues and organs are all fairly similar; as Lao Szu notes, "to an NMR machine, our bodies are like big bags of dirty water." However, modern MRI uses pulse sequences that distinguish different tissues in terms of their  $T_1$  and  $T_2$ . Let's examine how this is achieved:

The other phantom with 2 capillary tubes should be used. Examining it straight up from the bottom, it is seen that one capillary is blue – it has  $\text{CuSO}_4$  dissolved into the  $\text{H}_2\text{O}$ , reducing the  $T_1$  of the water in this capillary. The other capillary has pure  $\text{H}_2\text{O}$ , so its  $T_1$  is about 2 seconds.

First form an image with one  $90^\circ$  pulse repeating approximately every 6 seconds. Both tubes should appear with equal intensity (area in frequency domain). Then increase the repetition rate to one pulse per 0.5 seconds. The  $\text{CuSO}_4$  tube will recover fully, since its  $T_1$  is short. However, the pure  $\text{H}_2\text{O}$  will be partly saturated as the nuclear magnetization does not have sufficient time to relax between pulses. Now, in the image, one peak will be decreased in area. Rotation of the phantom by  $180^\circ$  in the probe should interchange the 2 peaks. Thus, not only can you tell there are 2 tubes (and how big each is and how far is the spacing), but you can tell that they are filled with different fluids (different  $T_1$ 's). You have made a  $T_1$ -weighted image. Too bad your leg won't fit into this thing!

## L. PHASE-SENSITIVE DETECTION

The mixer (also known as phase-sensitive detector) is a 3-port (two inputs and one output) analog, passive device. The output X is approximately the product of the L and R inputs. The L input is from the 60 MHz ( $\omega_0/2\pi$ ) oscillator. The R input is the amplified spin signal. Thus

$$L(t) = \cos \omega_0 t,$$

$$R(t) = a(t) \cos(\omega t + \delta).$$

Here  $a(t)$  is the time-varying amplitude (think of an FID or echo),  $\omega$  is the spin frequency  $\gamma H$ , and  $\delta$  is a phase-shift (there are long cables in the apparatus, long compared to the wavelength, so  $\delta$  is not known in advance). The output  $X$  is

$$X(t) = LR = a(t) \cos(\omega t + \delta) \cos(\omega_0 t).$$

Using the trigonometric identity,

$$\cos x \cos y = (1/2)[\cos(x+y) + \cos(x-y)],$$

$$X(t) = (a(t)/2)[\cos((\omega + \omega_0)t + \delta) + \cos((\omega - \omega_0)t + \delta)]$$

We pass the output through a low-pass filter, so we take the average over the high frequency ( $\omega + \omega_0$ , nearly  $2\pi$  times 120 MHz); the cosine averages to zero.

Thus, the time-average of  $X$  is

$$\langle X \rangle = (a(t)/2) \cos((\omega - \omega_0) t + \delta).$$

The output is at the difference frequency, the difference between the spin frequency and the 60 MHz oscillator. The time-varying amplitude  $a$  is present in the output. Overall, the mixer shifts the spin signal from 60 MHz +  $\Delta$  to simply  $\Delta$ .

## M. MEASURING DIFFUSION BY NMR

This is an advanced topic, extending the study of spin echoes. Here you will measure the diffusion coefficient (or diffusivity,  $D$ ) of water.

A good **introduction** to diffusion and **random walks** is the book by H.C. Berg, *Random Walks in Biology*. Also see Chapter 1 of F. Reif's text on statistical physics.

Consider a random walker (drunk starting at a lamppost) who takes a unit length step every second, randomly forward or backward. After 5 steps his displacement  $x_5$  might be  $+1-1-1-1+1 = -1$ . Note that  $x_{n+1} = x_n \pm 1$ .

Taking an ensemble average,  $\overline{x_{n+1}} = \overline{x_n} + 0$ , since the average of  $\pm 1$  is zero. By inductive reasoning, we see  $\overline{x_n} = 0$ ,  $\overline{x_{n+1}} = 0$ ; we are not surprised, because each step is as likely plus as minus. Squaring  $x_{n+1} = x_n \pm 1$  yields

$$x_{n+1}^2 = x_n^2 + 1 \pm 2x_n. \text{ Taking the ensemble average, } \overline{x_{n+1}^2} = \overline{x_n^2} +$$

$1 + 0$ . Thus, the mean **squared** displacement builds linearly in time. Again using inductive reasoning ( $n=0, n=1, n=2$ , etc.), we see  $\overline{x_n^2} = n$ . Note this is very unlike constant velocity, where the displacement itself (not squared) is linear in time.

Molecules in a gas or liquid move in such a fashion, being propelled "randomly" by their own thermal motion and their neighbors'. This diffusive motion is three dimensional, but

like the random walk, one expects  $\overline{\Delta x^2}$  to be proportional to time. This motion is what the botanist Brown saw and was labeled (by others) Brownian motion. The definition of D is

$$\overline{\Delta x^2} = 2Dt,$$

expressing the mean squared displacement during time interval t. The units of D are cm<sup>2</sup>/sec.

Diffusivity D decreases with increasing gas or liquid density. In a denser fluid, the diffusing molecule changes its direction more rapidly (roughly, one change for each collision). So the D of water is about  $2 \times 10^{-5}$  cm<sup>2</sup>/sec at 25°C, while D of helium atoms in helium gas (at 1 atmosphere) is about 2 cm<sup>2</sup>/sec. The value for helium is large because of the low number density, the small mass (and correspondingly high thermal velocity, with  $(1/2) m v_x^2 = 1/2 kT$ ), and the small size of the He atom (making collisions less frequent). Long mean-free paths translate into large values of D.

**NMR:** Consider the response of spins to a 90- $\tau$ -180- $\tau$ -echo pulse sequence, when there is a uniform field gradient applied to the sample. Between the two pulses, the spins de-phase; the 180° pulse flips the spins in such a way that they will come back into phase at time 2 $\tau$  (and generate a spin echo), **provided** they run at the same frequency during the de-phasing and re-phasing parts of the experiment. But if the spins can diffuse, each spin will have a different average location (and see a different average field and precess at a different average frequency) in the two halves (between 90 and 180 versus between 180 and echo). So the spins will not all be back in-phase, leading to a reduction in the echo amplitude.

Mathematically, we approximate that a spin has average location  $x_1$ , during the first half and  $x_2$  during the second half. Clearly, this is oversimplified; the spin does not jump from  $x_1$  to  $x_2$  at the instant of the 180 pulse. Anyway, recall there is a field gradient along the x-axis, so a spin at  $x_1$  sees  $H = Gx_1$  (as always, we are in a rotating frame so we can drop the uniform field from our equations) and precesses at  $\omega = \gamma H = \gamma Gx_1$ . During the first half of duration  $\tau$ , it accumulates precessional phase about the magnetic field of  $\Phi_1 = \omega\tau = \gamma G\tau x_1$ .

In the second half, the spin is taken to be at  $x_2$ , so it accumulates phase  $\Phi_2 = \gamma G\tau x_2$ . The total phase accumulated, from the first 90° pulse where the spins all start in-phase to the time of the echo, is  $\Phi_0 = \Phi_2 - \Phi_1$ . The crucial negative sign reminds you that the 180° pulse inverts the phase of the spins (or makes it seem the spins all precessed backwards during the first half). Thus  $\Phi_0 = \gamma G\tau(x_2 - x_1)$ . If there were no diffusion,  $x_2 - x_1$  would be zero for every spin and every spin would have  $\Phi_0 = 0$ . All the spins would be back in-phase at the echo time and the echo would be full amplitude. But if there is diffusion, then the spins will have a distribution of phases  $\Phi_0$ . The spins will not all be in-phase, so the vector sum will not be as large (the

echo will have less amplitude). This decrease in echo amplitude is how we can measure D using NMR.

Squaring the above equation and taking its ensemble average (there are lots of molecules in our sample),

$$\overline{\ddot{O}_0^2} = (\gamma G \tau)^2 \overline{(x_2 - x_1)^2}$$

Recall  $\overline{\ddot{A}x^2} = 2Dt$  and assume the motion from  $x_1$  to  $x_2$  occurs in a time interval of about  $\tau$ ,  $\overline{\Phi_0^2} = (\gamma G \tau)^2 2D\tau$ . So the mean-squared de-phasing grows as  $\tau^3$ .

How does this affect the signal amplitude? For a random variable  $\Phi_0$  with probability distribution  $P(\Phi_0)$ ,  $\overline{\cos \Phi_0} = \int P(\Phi_0) \cos \Phi_0 d\Phi_0$ .

And  $\cos \Phi_0$  is just the projection (in the NMR experiment) of the spins onto the x-axis in the rotating frame. Provided P is a Gaussian (normal) distribution centered about zero, like we have here,  $P(\Phi_0) \sim K e^{-b\Phi_0^2}$ , some integration yields:

$$\overline{\cos \Phi_0} = \exp(-\overline{\Phi_0^2} / 2).$$

So our echo amplitude M is  $M = \overline{\cos \Phi_0} = \exp(-\gamma^2 G^2 D \tau^3)$ . Now, had we done no approximation, but instead treated the position x of the spin as changing continuously, we would have obtained the **correct** answer,

$$M = \overline{\cos \Phi_0} = \exp(-\gamma^2 G^2 D \tau^3 2/3),$$

which is almost the same.

Please take the time to check the dimensions of the argument of the exponential. You will find the argument is properly dimensionless. You can find the dimensions of  $\gamma$  from  $\omega = \gamma H$ .

**Experiment:** Put the tube of H<sub>2</sub>O into the magnet with the spinning air off. Create a gradient by mis-adjusting by 4 turns or 9 turns the Z shim knob; record the setting for later measurement of G. Measure the amplitude M of the spin-echo as a function of  $\tau$  for a wide range of delays  $\tau$ .

Fit the data M with the equation below:

$$M = A \exp(-2\tau/T_2 + -\gamma^2 G^2 D \tau^3 2/3),$$

which combines the expected amplitude decreases due to  $T_2$ -relaxation and diffusion. The constant  $A$  is just the amplitude extrapolated to zero  $\tau$ ; you can treat it as a fitting parameter. For  $T_2$ , just use  $T_2=T_1$  (use  $T_1$  for water that you measured earlier; this should be about 2 seconds); this reduces the number of fitting parameters. The horizontal axis of your plot is  $\tau^3$ . The value of  $\gamma$  for H nuclei is  $2\pi$  times  $4257.7 \text{ s}^{-1}$  per Gauss.

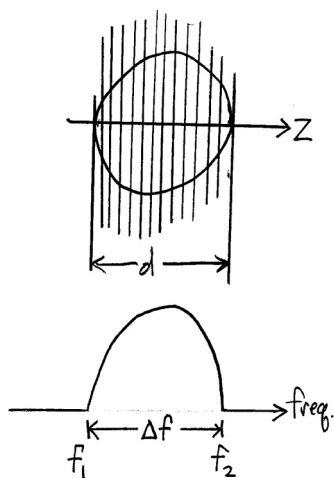
One way is to remove the  $T_2$  attenuation from your data, according to

$$M' \equiv M \exp(+2\tau/T_2) = A \exp(-\gamma^2 G^2 D \tau^3 / 3).$$

Thus, taking the natural log of the corrected signal  $M'$  gives

$\ln M' = \ln A + (-\gamma^2 G^2 D / 3) \tau^3$ , which is slope-intercept form. In a plot of  $\ln M'$  versus  $\tau^3$ , the slope is  $-\gamma^2 G^2 D / 3$ ; all the factors are known except  $D$ , so  $D$  can be found from the experimentally determined slope.

We have glossed over one issue, the value of  $G$ . You can find  $G$  by measuring the spectrum of a known-size sample in that  $z$ -gradient. With water (a single resonance line) in a tube of inner diameter  $d$  (see Figure 8), two points at opposite ends of the



*Figure 8: Spectrum of round tube of diameter  $d$  of water in gradient  $G$ . The object is pictured as having many slices normal to  $z$ , so the spectrum is the projection onto the  $z$ -axis.*

diameter (parallel to  $z$ -axis) are spaced by  $d$ , so they see fields differing by  $Gd$ , and their precession frequencies (in Hertz) differ by  $(\gamma/2\pi)Gd$ . Thus,  $f_2 - f_1 = \Delta f = \Delta\omega/2\pi = \gamma\Delta H/2\pi = \gamma G\Delta Z/2\pi = \gamma Gd/2\pi$ . The spectrum should be analyzed to find  $\Delta f$ , as in Figure 8. Of course, you want to use the field shift knob so all the spins are above or below 60.0 MHz, to avoid the spectrum folding-over on itself. Please refer to section III K on NMR imaging. To measure the tube's inner diameter, go to the shop and find the largest drill bit that can enter the tube; then use calipers to

---

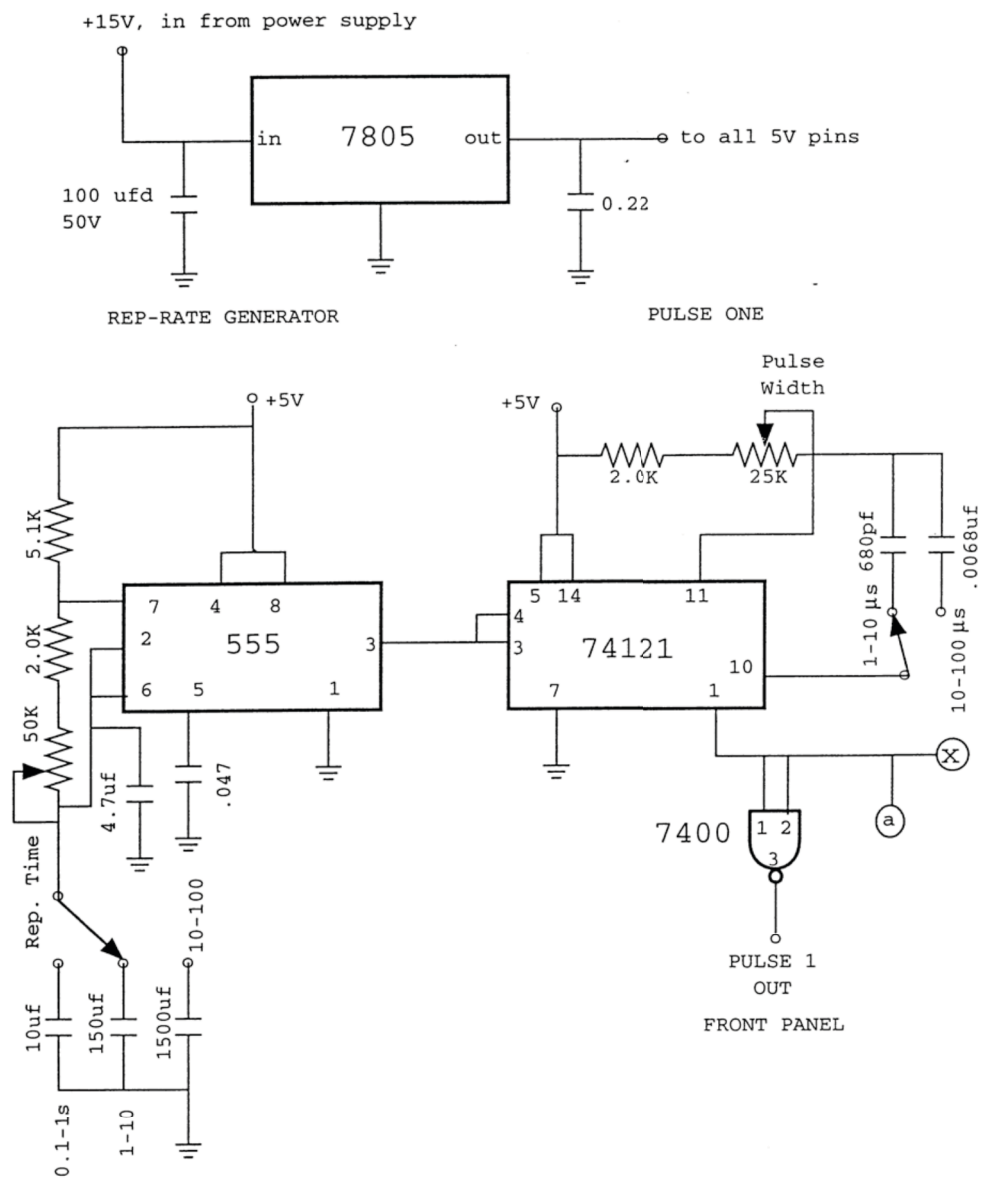
measure the drill bit. Wipe off all foreign material (like steel particles) before touching drill bit to sample tube.

You should measure G at 2 settings of the z-shim knob and measure D for each value of G. Writing down the knob setting will allow you to first measure both G values and then later do both echo measurements to determine D.

## APPENDIX I. Circuit Diagrams

### NMR PULSE GENERATOR

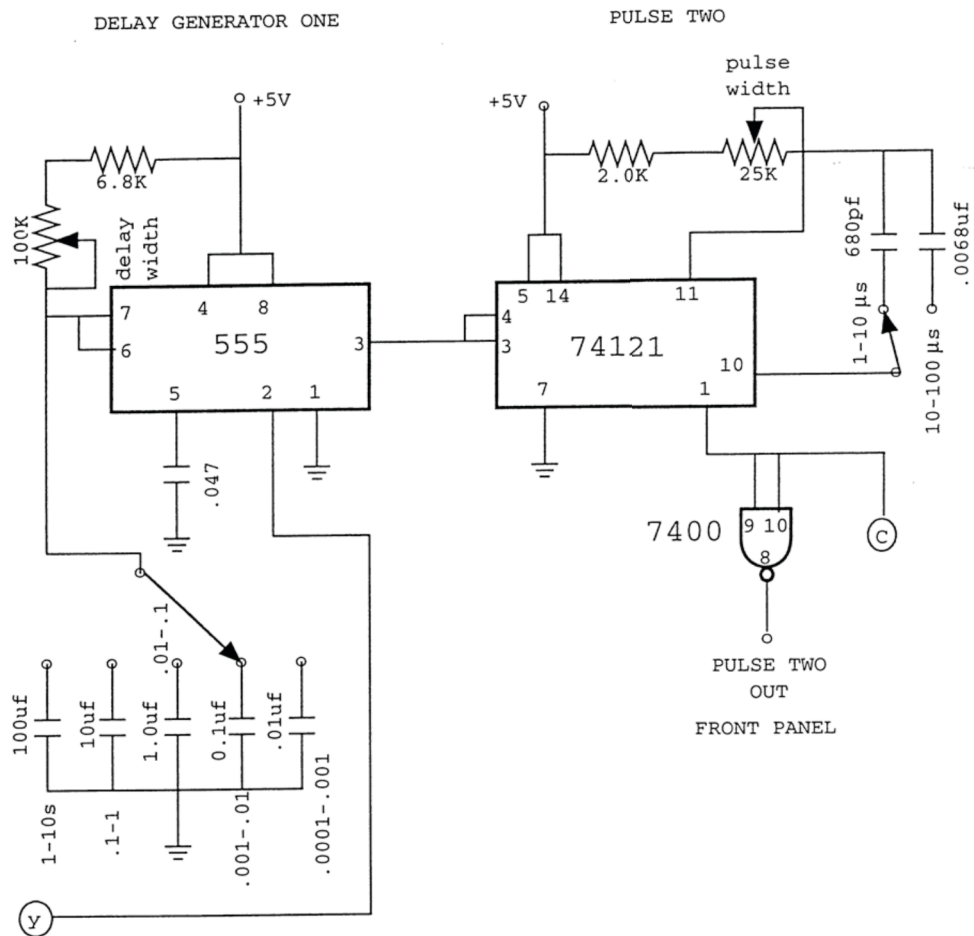
#### Repetition Rate Generator, Pulse One





# NMR PULSE GENERATOR

## Delay Generator One, Pulse Two

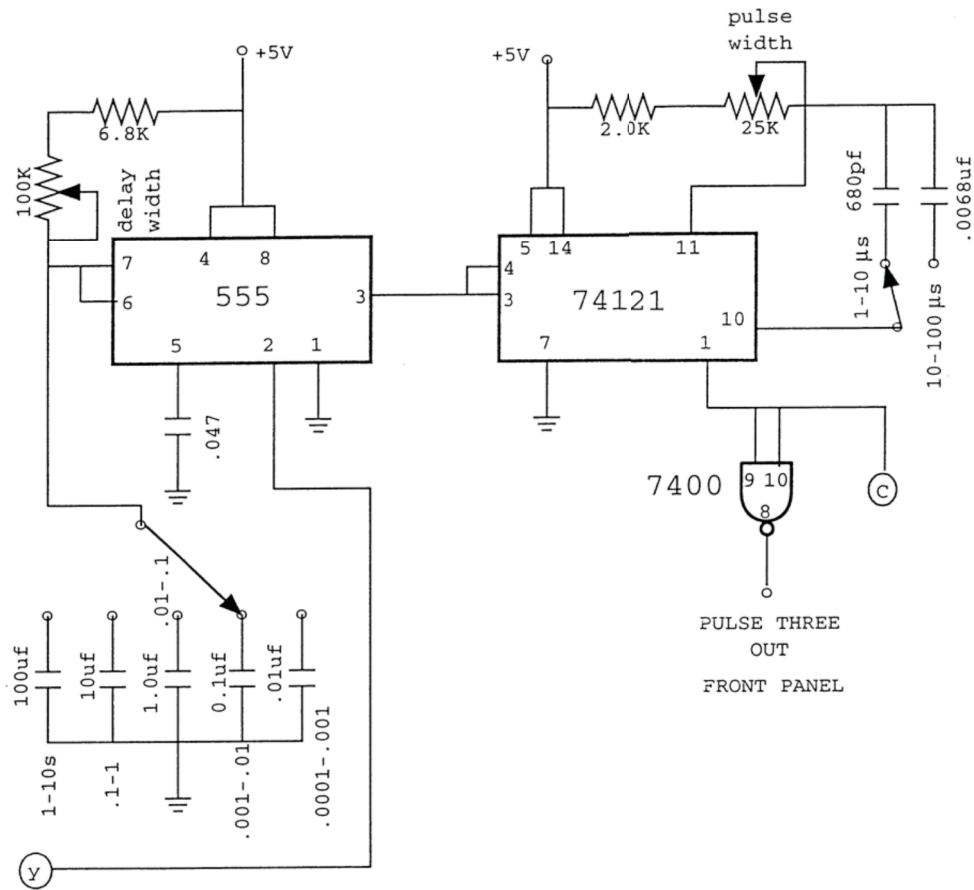


# NMR PULSE GENERATOR

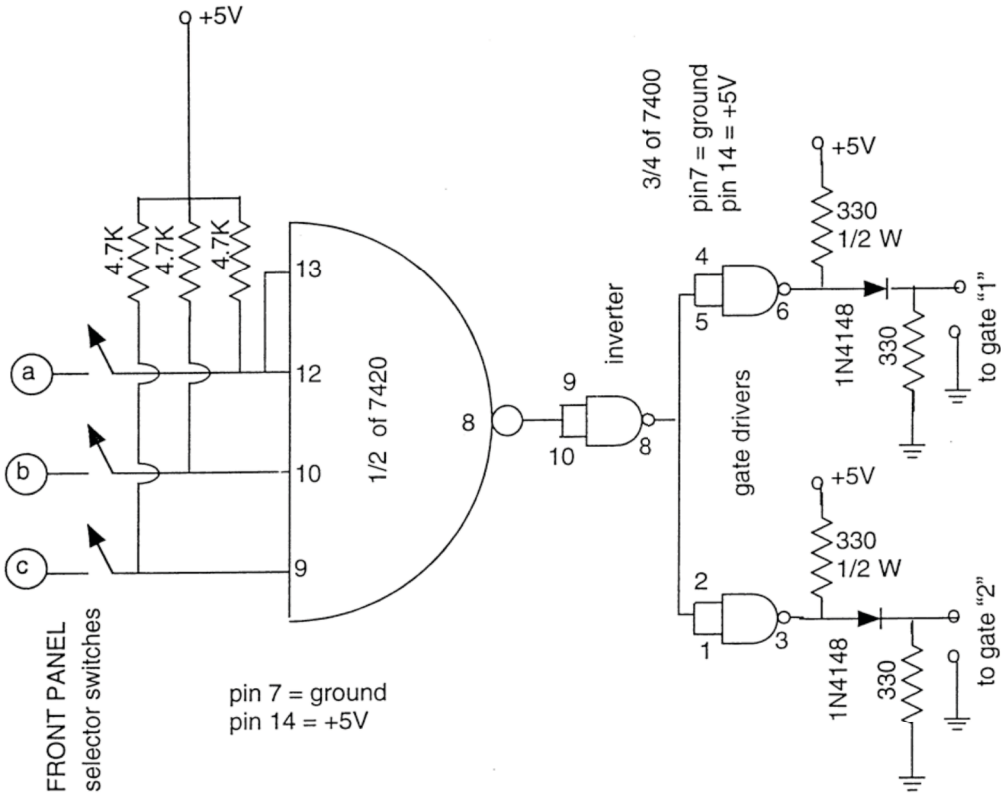
## Delay Generator Two, Pulse Three

DELAY GENERATOR TWO

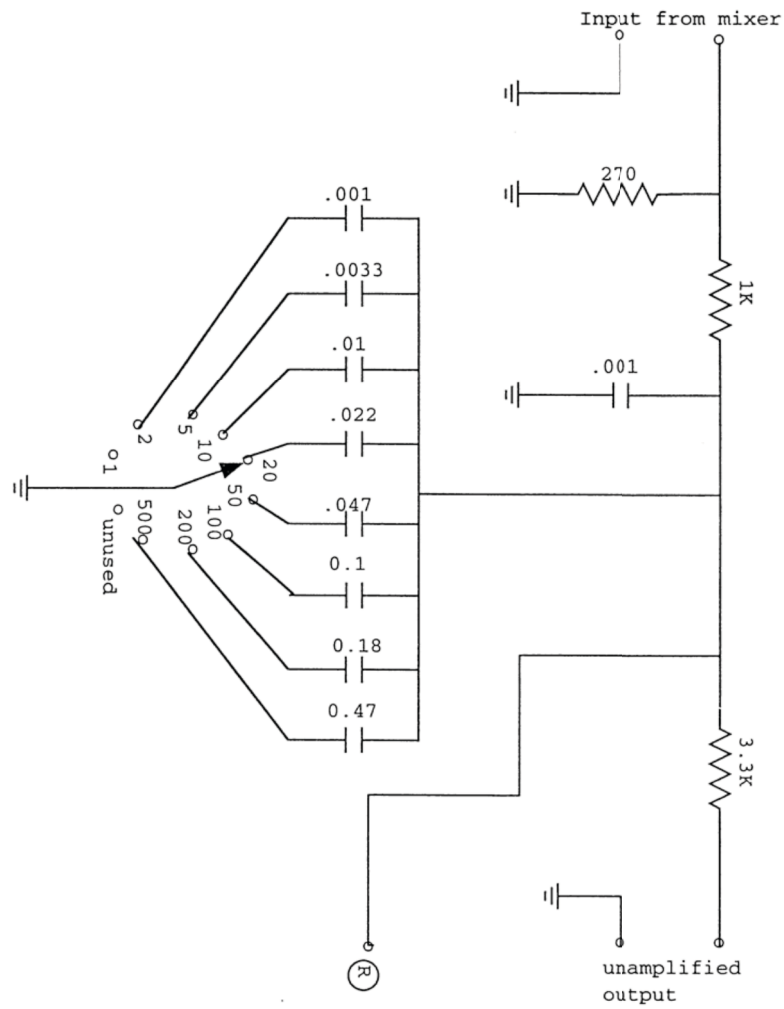
PULSE THREE



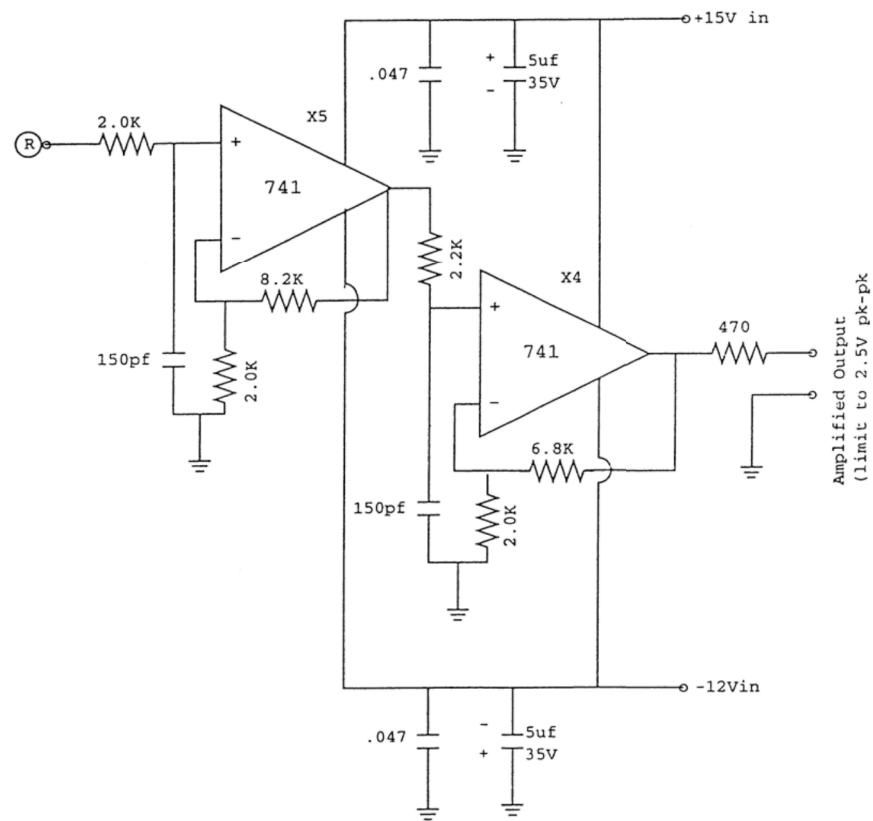
## CIRCUIT TO DRIVE MIXER GATES



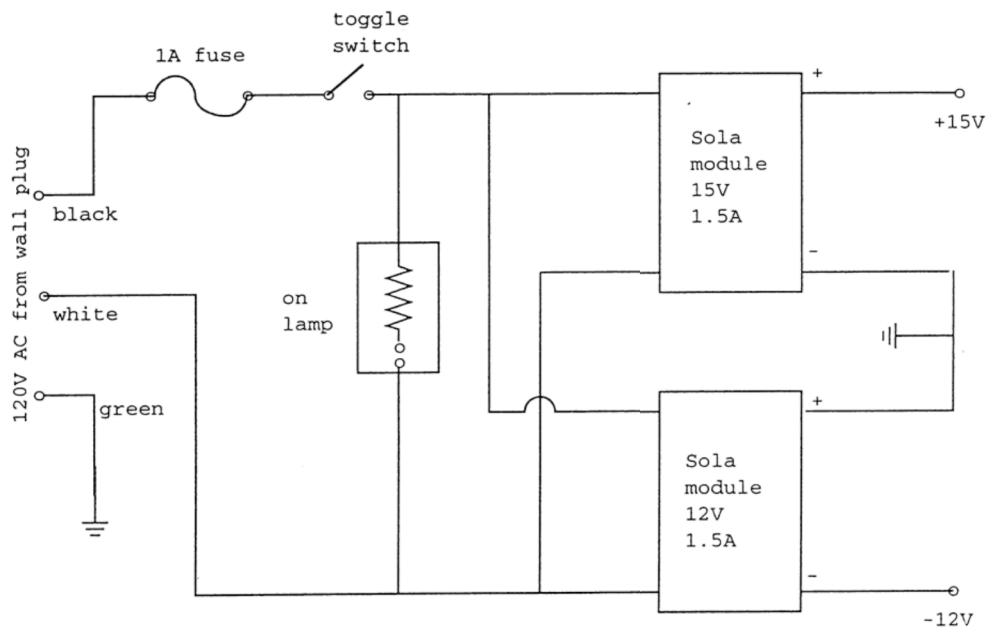
# LOW PASS FILTER CIRCUIT

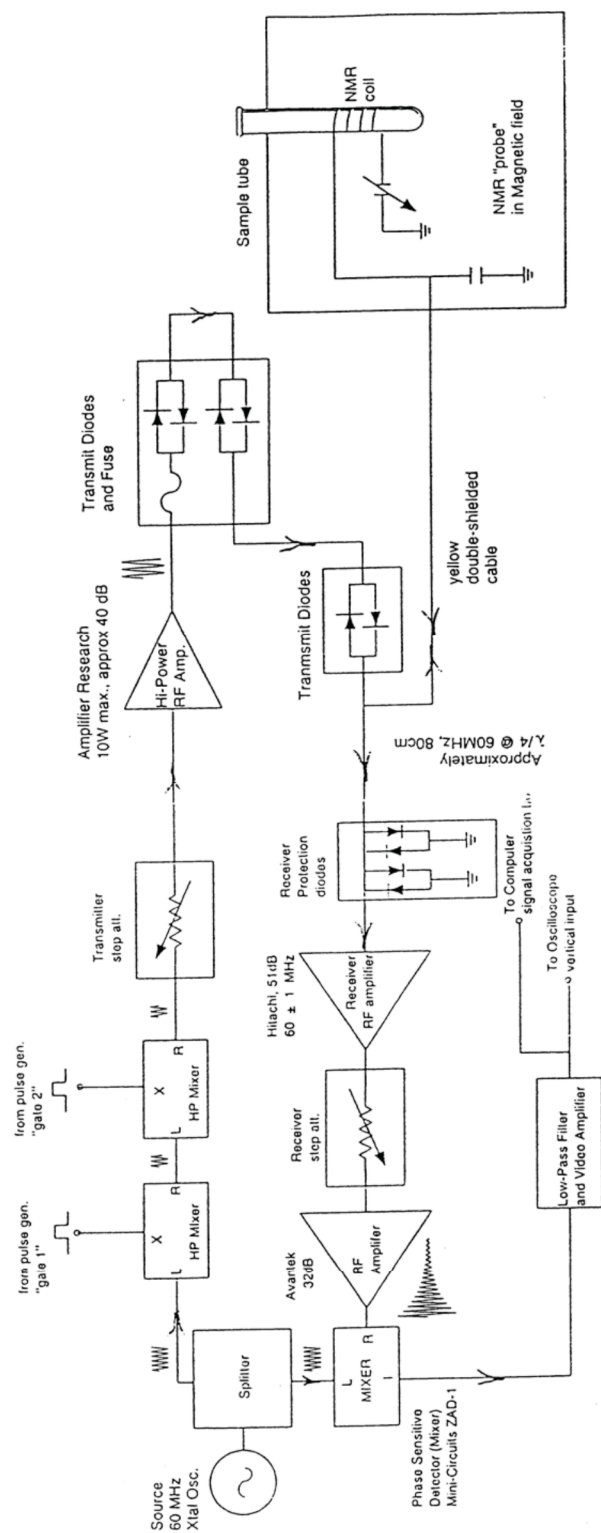


# VIDEO AMPLIFIER CIRCUIT



## POWER SUPPLY CIRCUIT





60 MHz NMR Block Diagram